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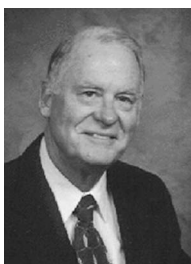
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Larry C. Andrews is Professor Emeritus of Mathematics at the University of Central Florida and an associate member of the College of Optics/CREOL. He is also an associate member of the Florida Space Institute (FSI). Previously, he held a faculty position at Tri-State University and was a staff mathematician with the Magnavox Company, antisubmarine warfare (ASW) operation. He received a doctoral degree in theoretical mechanics in 1970 from Michigan State University. Dr. Andrews is a Fellow of SPIE and has been an active researcher in optical wave propagation through random media for more than 30 years and is the author or coauthor of twelve textbooks on topics of differential equations, boundary value problems, special functions, integral transforms, wave propagation through random media, and mathematical techniques for engineers. Along with wave propagation through random media, his research interests include special functions, random variables, atmospheric turbulence, and signal processing.



Ronald L. Phillips is Professor Emeritus at the University of Central Florida. He holds appointments in the Department of Electrical Engineering, Mathematics, and the Townes Laser Institute in the College of Optics/CREOL. He has held positions on the faculties at Arizona State University and the University of California. He received a doctoral degree in Electrical Engineering in 1970 from Arizona State University. Dr. Phillips has been an active researcher in the area of wave propagation through random media for more than 38 years. He was awarded a Senior NATO Postdoctoral Fellow in 1977 and the American Society for Engineering Education 1983 Medal for Outstanding Contributions in Research. Dr Phillips is a SPIE Fellow, OSA Fellow, and an AIAA Fellow. He is the coauthor of three books on wave propagation through random media and a text book on mathematical techniques for engineers. He has taught industry short courses on the topic of propagation through turbulence and its effects on free-space optical systems for the last 15 years. In addition to optical wave propagation, his research interests include free space optical communications, active imaging, and laser radar.