Effect of fabrication tolerances on the performance of two-dimensional polymer photonic crystal channel drop filters: a theoretical investigation based on the finite element method

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Abstract. Guidelines for the design and fabrication of polymer photonic crystal channel drop filters for coarse wavelength division multiplexing are provided. A Fabry-Perot cavity consisting of a membrane-type slab photonic crystal, where a hole row perpendicular to the propagation direction is removed, is considered. We selected nanoimprinting as the manufacturing technique. The influence on the cavity performance of several key parameters, i.e., polymer core material, lattice geometry, defect length, and holes’ radius, has been investigated in a device compliant with the requirement of the ITU-T G.694.2 standard. A detailed analysis of the fabrication tolerances has been carried out at 1551 nm. The maximum acceptable drift of the geometrical parameters has been accurately evaluated by using the finite element method to prove that the fabrication tolerances do not significantly affect the performance of polymer filters for coarse wavelength division multiplexing, when manufactured by thermal nanoimprinting lithography. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.OE.52.9.097104]

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1 Introduction
For more than one decade, photonic-crystal slabs have been identified as one of the most promising photonic crystals (PhCs) configurations due to their high design flexibility and the possibility of fabricating them through the well-established planar technology, and several high-performance devices have been demonstrated. The wavelength of the defect modes in PhC slabs can be identified by tailoring both size and shape of defects. This allows one to design and fabricate microcavities covering a wide range of applications in the field of low-threshold lasers, channel drop filters, and chemical sensing. Fabry-Perot cavities, made by a couple of two-dimensional (2-D) photonic bandgap mirrors separated by an unperturbed region, have been widely investigated.

Although silicon and III-V semiconductors are the mostly used materials for planar PhCs, polymer PhC slabs are emerging as a valid alternative because of some interesting advantages such as low cost, readies of functionalization with biochemical receptors, and low optical loss.

One of the most promising applications of 2-D PhC cavities is in the field of coarse wavelength division multiplexing (CWDM), which is a well-established technology for short-haul, enterprise, and metro optical networks demanding next-generation chip-scale photonic components having high reliability and low cost.

In this paper, we study the fabrication tolerances of a channel drop filter for CWDM, which is compliant with the requirement of the ITU-T G.694.2 standard (pass-band width of each channel = 13 ± 3 nm, channel spacing = 20 nm). The device (see Fig. 1) is based on a polymer PhC structure incorporating a linear defect in the lattice along the propagation direction. The defect allows photonic states to be highly confined in the band gap, thus leading to a narrow-band filtering operation. The PhC is obtained through a 2-D periodic pattern of holes in a polymer air-suspended membrane and the two separate PhC reflectors in the structure are the mirrors of the Fabry-Perot cavity. Each reflector includes p columns and q rows. The values of both p and q have been selected aiming at a compromise between two opposite crucial requirements, i.e., the filter footprint minimization and maximization of the performance.

We denote the defect length, the lattice constant, and the hole radius with d, a, and r, respectively. Nanoimprinting lithography, which allows a cost-effective and high throughput manufacturing of nanoscale devices, has been envisaged for the filter fabrication. In literature, the devices that are quite similar to the investigated one have been fabricated by e-beam lithography and reactive ion etching, focused ion beam etching, and nanoimprinting lithography. We believe that the latter fabrication technique is the most suitable, especially because of its low cost.

Since our device is based on an air-suspended membrane and its performance is not significantly affected by the thickness of the polystyrene slab, which is not taken into account by the 2-D calculation methods, the device has been modeled by using the 2-D finite element method (FEM), which...
assures a good trade-off between results accuracy and computation time. We have also verified that the results obtained by 2-D FEM are close (difference <5%) to those of the 3-D FEM, especially for the resonance wavelength and transmission. A conservative evaluation of the quality factor has been demonstrated by the 2-D simulations when compared to the more accurate three-dimensional ones.

Some thermoplastic polymers with different refractive index, i.e., polytetrafluoroethylene, \( n = 1.30 \), polyvinylidene fluoride, \( n = 1.42 \), polymethyl methacrylate (PMMA), \( n = 1.49 \), and polystyrene, \( n = 1.59 \), have already been evaluated by the authors for the membrane realization. Those polymers, especially PMMA and polystyrene, are the most used in nanoimprinting lithography because their viscosity can be easily changed to a large extent by only varying the temperature. The results reported in Refs. 21 and 22 allowed us to identify polystyrene as the most appropriate material because, among the four investigated polymeric materials, it is the only one allowing the formation of a complete bandgap for in-plane propagation directions. Moreover, polystyrene exhibits an excellent film quality. We assumed the polystyrene layer as deposited on an \( \text{SiO}_2 \) film laying on a silicon substrate. The air-suspended membrane can be realized by selectively removing the \( \text{SiO}_2 \) underneath the polystyrene.

We have selected the square lattice of the planar PhC because it provides the highest value of attenuation within the bandgap in comparison with the hexagonal and the honey-comb lattices.

Useful guidelines for the design and manufacturing of CWDM channel drop filters based on the investigated structures are provided in this paper. In particular, we have first designed a channel drop filter with central wavelength equal to 1551 nm, a pass-band width compliant with the target application, and low insertion loss. Then we evaluated the effect of random variations in the hole radius/shape, the lattice constant, and the defect length on the device performance. By using that approach, the fabrication tolerances have been estimated.

![Fig. 1] Configuration of the channel drop filter. \( d \) is the defect length, \( a \) is the lattice constant, \( r \) is the hole radius, \( p \) and \( q \) are the number of columns and rows, respectively.

Only a few preliminary results of the filter design, i.e., the dependence of the component performance on the defect length, were reported and briefly discussed in Ref. 23.

2 Design

The target central wavelength of the designed filter is 1551 nm, which is one of the wavelengths defined by the G.694.2 CWDM wavelength grid. According to that standard, the pass-band width of each channel is 13 ± 3 nm. Therefore, the cavity \( Q \)-factor should be in the range from 97 to 155. The aims of our design are both the fulfillment of those requirements and the maximization of the resonance transmission, which strongly influences the device insertion loss.

We initially assumed \( a = 620 \) nm, \( p = 7 \), and \( q = 8 \).

The dependence of the cavity resonance wavelength on the hole radius for several values of the defect length is shown in Fig. 2. As in all Fabry-Perot cavities where the resonance wavelength is proportional to the resonator length, the resonance wavelength of our PhC cavity increases as \( d \) increases. As typical in all PhC cavities, in our device, the electromagnetic field at resonance is confined in both the defect region having length \( d = d \) and the holes of the rows close to the defect region. Since the resonance wavelength is proportional to the average refractive index of the medium where the field is confined at resonance, the radius of the air holes increases as the average index decreases, and thus the resonance wavelength decreases, too.

In the considered range of \( r \) values, ranging from 0.38 to 0.44, the fulfillment of the specification on the filter central wavelength implies a \( d \) value ranging from 1.18 to 1.32.

It is well known that high \( Q \)-factor and high resonance transmission \( T \) are conflicting requirements. Both \( Q \) and \( T \) versus the hole radius are shown in Fig. 3. The \( Q \)-factor increases as the hole radius increases, while \( T \) decreases when \( r \) increases. The \( Q \)-factor monotonically increases as \( d \) increases, while \( T \) monotonically decreases as \( d \) increases.

A good trade-off between the resonance transmission and the \( Q \)-factor can be achieved for \( r = 0.39 \) and \( d = 1.2a \). For those geometrical parameters, the \( Q \)-factor is 115 (target range = 97 to 155) and the resonance transmission is >50%. For \( r = 0.39a \) and \( d = 1.2a \), the filter central wavelength is

![Fig. 2] Cavity resonance wavelength versus hole radius for several values of \( d \). Lattice constant = 620 nm, \( p = 7 \), \( q = 8 \). Dots are data points, while lines are fitting curves.
equal to the target one, i.e., 1551 nm, and the device footprint is $113.6a^2$ ($=43.7 \mu m^2$).

We have verified that the assumed values of $p$ and $q$ ($p = 7$ and $q = 8$) are a good compromise between the performance enhancement and the footprint minimization. In fact, the increase of the column/row numbers implies an improvement of the $Q$-factor and a decrease of $T$. Moreover, it obviously causes an increase of the device area. As $p$ and $q$ decreases, $T$ slightly increases and $Q$ significantly decreases. For example, for $p = 9$ and $q = 10$, the $Q$-factor is 240 and $T = 46\%$, while for $p = 5$ and $q = 6$, we have $Q = 50$ and $T = 54\%$.

As already mentioned, we have initially assumed $a = 620$ nm for studying the influence of the hole radius and the defect length on the filter features. We have also demonstrated that this value of $a$ provides the best device performance, fulfilling the requirement of the ITU-T G.694.2 standard.

In Figs. 4(a) and 4(b), both $Q$ and $T$ versus the lattice constant have been reported for several $d$ values, suitably selecting the hole radius to obtain a resonance wavelength at 1551 nm. We have considered a range of $a$ from 580 to 640 nm to provide a $Q$-factor in the target range ($97 < Q < 155$). Higher values of $a$ have not been considered because the device fabrication is impossible for holes that are too large.

For each couple of $a$ and $d$ values, the radius allowing a resonance wavelength of 1551 nm is shown in Fig. 4(c). The holes’ radius value allowing the fulfillment of the

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**Fig. 3** (a) Quality factor dependence on the hole radius for several values of the defect length. (b) Resonance transmission versus hole radius for $d = 1.1a$, 1.2$a$, 1.3$a$, and 1.4$a$. Lattice constant = 620 nm, $p = 7$, $q = 8$. Dots are data points, while lines are fitting curves.

**Fig. 4** (a) Quality factor and (b) resonance transmission dependence on the lattice constant for several values of the defect length with a suitable size of the hole radius to obtain the resonance condition at 1551 nm. The green areas represent the case studies compliant with the target range of the $Q$-factor. (c) Holes radius allowing the fulfillment of the requirement on the resonance wavelength for each couple of $a$ and $d$ values. Dots are data points, while lines are fitting curves.
requirement on the resonance wavelength increases as the lattice constant \(a\) and/or the defect length \(d\) increase.

Results in Figs. 4(a) and 4(b) confirm that high \(Q\)-factor and high resonance transmission \(T\) are conflicting requirements. If we consider only the combinations of the geometrical parameters allowing the fulfillment of the constraint 97 < \(Q\) < 155 (green area), the condition \(a = 620\) nm, \(d = 1.2a\), and \(r = 0.39a\) provides the highest value of \(T\), thus minimizing the insertion loss of the filter.

3 Fabrication Tolerances

The fabrication tolerances have been evaluated by investigating the effect of random variation in the filter geometry due to the potential fabrication imperfections on the cavity performance such as the resonance wavelength, the \(Q\)-factor, and the resonance transmission. In particular, we have randomly perturbed the hole radius, the lattice constant, the defect length, and the circular shape of the holes and have observed the impact of that perturbation on the performance parameters. The perturbations have been chosen so that their average value is zero, using a Gaussian random generator.

We have simulated a lot of cavities to investigate the impact on the filter performance of random variation in the hole radius. The holes of each resonator have a radius \(r^*\), which is equal to

\[ r^* = r + \rho, \]

where \(r = 0.39a\) (=242 nm) is the nominal value of the radius and \(\rho\) is the random perturbation term, which is obtained by a Gaussian random generator whose parameters are mean value = 0 and standard deviation = \(\sigma_r\). For each filter, we have calculated the resonance wavelength, the \(Q\)-factor, and the resonance transmission. As an example, the dependence of the average value of both \(Q\) and \(T\) on the standard deviation \(\sigma_r\) is shown in Fig. 5. The average value of both the \(Q\)-factor and the resonance transmission decreases as the standard deviation \(\sigma_r\) increases, as expected. This means that a reduction of the uniformity of the holes radius implies a filter performance degradation. The \(Q\)-factor decrease is quadratic, while the \(T\) decrease is linear.

The histograms of the values of the \(Q\)-factor and the resonance wavelength for three values of \(\sigma_r\), i.e., 2.5, 10.0, and 17.5 nm, are shown in Fig. 6. For \(\sigma_r = 2.5\) nm, almost all the simulated filters (≈95%) have a resonance wavelength in the range 1548 to 1554 nm and a \(Q\)-factor >97. When \(\sigma_r\) increases, the percentage of filters with a resonance wavelength in the range 1548 to 1554 nm and a \(Q\)-factor >97 decreases. For \(\sigma_r = 17.5\) nm, only 23% of the filters have a resonance wavelength in that range. On the basis of the specification assumed for the central wavelength and...
assuming a target production yield >70%, we have derived that the fabrication tolerance allowed on the hole radius is equal to ±5 nm. This means that if the fabrication process is able to guarantee holes with a radius of 242 ± 5 nm, at least 70% of the produced device will be compliant with the requirements of the ITU-T G.694.2 standard.

By using the same simulation technique described for the hole radius, we have evaluated the fabrication tolerance on the lattice constant. The uniformity of the lattice constant values is taken into account by the standard deviation \( \sigma_r \). The simulation results have shown that the uniformity in the values of lattice constant decreases when \( \sigma_r \) increases. Figure 7 shows the histograms of the values of both the \( Q \)-factor and the resonance wavelength for three values of \( \sigma_r \), i.e., 10, 20, and 30 nm. For \( \sigma_r = 10 \text{ nm} \), the predicted production yield is close to 80%. Assuming a target production yield >70%, the fabrication tolerance on the lattice constant has to be ±12 nm.

From both Figs. 6 and 7, we can conclude that the most critical performance parameter is the resonance wavelength. For example, for \( \sigma_r = 10 \text{ nm} \), all the simulated filters have a \( Q \)-factor >97, while only 30% of the devices has a resonance wavelength ranging from 1548 to 1554 nm.

By investigating with the same approach the fabrication tolerance on the defect length, we have concluded that it is equal to ±4 nm. Finally, we have studied the effect of any perturbation of the circular shape of the holes. We have assumed that the fabrication imperfections may cause elliptical holes with a random eccentricity (when the eccentricity is zero, the ellipse degenerates in a circle). Our simulations allow us to conclude that the fabrication tolerance on the eccentricity is 0.06.

Both the parameters of the designed filter and the fabrication tolerances are summarized in Table 1. The performance of designed filter, in terms of \( Q \) and \( T \), is comparable to the one exhibited by the fabricated cavities based on the same technology, which are reported in the literature.18,19

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Nominal Value</th>
<th>Fabrication Tolerance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lattice constant (nm)</td>
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</tr>
<tr>
<td>Defect length (nm)</td>
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<tr>
<td>Hole radius (nm)</td>
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<tr>
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<tr>
<td>Rows number</td>
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</tr>
<tr>
<td>Quality factor</td>
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<td>—</td>
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<tr>
<td>Resonance transmission (%)</td>
<td>( T )</td>
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<td>—</td>
</tr>
<tr>
<td>Central wavelength (nm)</td>
<td>—</td>
<td>1551</td>
<td>—</td>
</tr>
<tr>
<td>Device footprint (( \mu \text{m}^2 ))</td>
<td>—</td>
<td>43.7</td>
<td>—</td>
</tr>
</tbody>
</table>

4 Conclusions

Guidelines for the design and the fabrication of optical filters for CWDM applications based on a Fabry-Perot cavity in a polymer planar PhC are reported in this paper. They are derived by FEM simulations and are relevant to a number of crucial aspects such as the materials to be used, the holes’ radius/shape, the defect length, and the lattice configuration. Assuming that the device is fabricated through the nanoimprinting technique, a channel drop filter compliant with the ITU-T G.694.2 standard has been studied with particular attention to the fabrication tolerances. For the hole radius and the lattice constant, we have estimated a fabrication tolerance of ~2%, while the fabrication tolerance on the defect length, which is the most critical geometrical parameter, is close to 0.5%. Assuming that fabrication imperfections can lead to elliptical holes, the fabrication tolerance on the ellipse eccentricity has been evaluated as equal to 0.06. Since those tolerances are compliant with the resolution of the thermal nanoimprinting lithography,24 the achieved results point out the attractiveness of polymer PhC filters in the context of CWDM.

CWDM drop filters that are available in the market are manufactured by either the silica planar lightwave circuit technology or the fiber technology. Those devices have a good reliability and a satisfactory thermal stability in the
range 0 to 70°C. The insertion loss of those filters ranges from 1 to 3 dB and the adjacent channel isolation is of the order of 30 dB. The device that we have studied is surely more compact than the ones available in the market because its footprint is only 44 μm², while the insertion loss/adjacent channel isolation of our filter are comparable to the ones exhibited by the components in the market. Experimental investigations, which will be our future work, are necessary to confirm that evaluation.

References


Francesco Dell’Olio received, in 2005 and 2010, his master’s degree (cum laude) in electronic engineering and his PhD in information engineering both from the Politecnico di Bari, Italy. His research interests include the fields of integrated optical sensors, especially angular velocity and chemical sensors, silicon photonics, and InP-based photonic integrated circuits. He is the coauthor of a book published by Springer, 20 papers published in international refereed journals, and more than 40 papers published in conference proceedings. His papers have been cited about 400 times and his h-index is 9. He is a member of OSA, and he serves as reviewer for several high impact factor journals such as Optics Express, Optics Letters, and IEEE Photonics Journal. Finally, he has been involved in several research projects on miniaturized optical gyroscopes, optical links for data handling on-board of satellites, sensor systems for harsh environments monitoring, and electromagnetic field photonic sensors.

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